January Regional

a) 5

b) 8

Choice (e) on all questions is "NOTA" which means "None Of The Above answers is correct."

1.	Simplify the following numerical expression: $2+16 \div 3-5+6 \div \frac{2}{3}$.						
	a) 10	b) 61/3	c) 111/3	d) -71/3	e) NOTA		
2.	Which of the following is an example of the Commutative Property of Multiplication?						
	a) $a(b+c)=(c+b)\cdot a$ c) $a(b+c)=(b+c)\cdot a$		b) $a(b+c) = a(b+c)$ d) $a(b+c) = a(b+c) + 0$		e) NOTA		
3.	Solve the equation $3(3x+1)-(x-1)=6(x+10)$. What is the sum of the digits of the value of x?						
	a) 13	b) 11	c) 10	d) 3	e) NOTA		
4.	Solve for y in terms of m: $16(y-m) = 4(2m-y)$.						
	a) $y = 3m$	b) $y = \frac{6}{5}m$	c) $y = \frac{3}{4}m$	d) $y = \frac{9}{10} m$	e) NOTA		
5.	The larger of two consecutive odd integers is four less than one-third of the smaller. Find the product of these two integers.						
	a) 99	b) 63	c) 35	d) no solution	e) NOTA		
6.	What is the sum of the integral solutions of the conjunction $-6 < 5x - 4 < 10$?						
	a) 0	b) 3	c) 6	d) 10	e) NOTA		
7.	Simplify the express	Simplify the expression: $(-2x)(-3xy)^3 + (3x)^2(xy)^2(-6y)$.					
	a) $-108x^4y^3$	b) $-36x^4y^3$	c) $-18x^4y^3$	d) $108x^4y^3$	e) NOTA		
8.	Factor the trinomial $6x^2 - 47x - 63$ into the form $(Ax + B)(Cx + D)$; what is the value of $A + B + C + D$?						

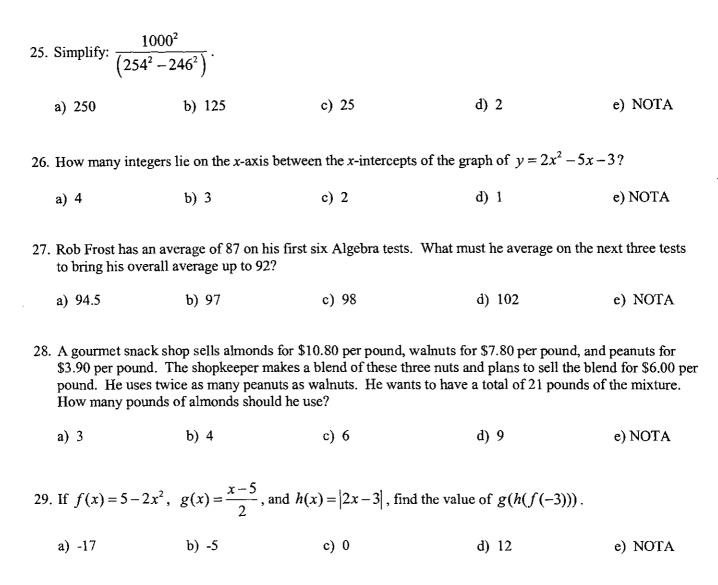
c) 13

d) -11

e) NOTA

9.	Which of the following is a factor of the polynomial $ax - 6xy - 5a + 30y$?						
	a) $(y+5)$	b) $(a-6y)$	c) $(a+6x)$	d) (y-5)	e) NOTA		
10. Factor completely: $x^4 - 81$.							
	a) $(x^2-9)(x^2+9)$		b) $(x^2+9)(x+3)(x-3)$	3)			
	c) $(x-3)^4$		d) $(x+3)^2(x-3)^2$		e) NOTA		
11	11. The binomial $3x-5$ is multiplied by its conjugate. That product is then subtracted from the square of the original binomial. Find the value of the resulting expression, given that $x = 5$.						
	a) 100	b) 0	c) -50	d) -100	e) NOTA		
12	12. The units digit of a two-digit number is 2 more than the tens digit. If the digits are reversed, the new number is 39 less than twice the original number. What is the product of the digits of the original number?						
	a) 8	b) 12	c) 35	d) 57	e) NOTA		
13	. The ratio of cats to o many are dogs?	logs to turtles in a pet s	tore is 4:7:1. There is a to	otal of 84 of these three	animals. How		
	a) 12	b) 21	c) 35	d) 49	e) NOTA		
14	$+3x^3+x-5.$						
	a) -10	b) -1	c) 0	d) 1	e) NOTA		
15	15. Simplify the expression $\left\{ \left[-\frac{1}{2} + \frac{3}{5} + \frac{2}{3} \left(1 - \frac{7}{10} \right) \right] \div \frac{1}{3} - \frac{1}{9} \right\}$. What is the absolute value of the difference of the numerator and denominator of the value of the given expression?						
	a) 19	b) 21	c) 89	d) 91	e) NOTA		
16	16. A new game called Ultimate Mu has started to get popular!! Teams earn either 4 or 7 points, depending on where they score from. What is the largest number of points which could not possibly be earned by a team playing Ultimate Mu?						
	a) 9	b) 17	c) 31	d) 111	e) NOTA		

17.	. How many digits were used in numbering the pages of Harry Potter and the Deathly Hallows, which total of 759 pages?							
	a) 2,164	b) 2,165	c) 2,168	d) 2,169	e) NOTA			
18.	18. If $32^x = 16$, then $x = ?$							
	a) -2	b) ½	c) ² / ₃	d) ⁴ / ₅	e) NOTA			
19.	19. For what value of x does the line with slope $-\frac{3}{2}$ pass through the points $(x, -1)$ and $(-2, 4)$?							
	a) 0	b) 4/ ₃	c) 11/ ₄	d) $\frac{3}{4}$	e) NOTA			
20.	20. What is the y-coordinate of the point of intersection of the graphs of $2x - 3y = 8$ and $2x + 4y = 2$?							
	a) $-\frac{6}{7}$	b) 2	c) 6	d) 10	e) NOTA			
21.	21. The point (6, -5) lies on line L which is perpendicular to the line whose equation is $3x - \frac{1}{5}y = 3$. What is the x-intercept of line L ?							
	a) (1, 0)	b) (23,0)	c) (-69, 0)	d) $\left(-\frac{23}{5}, 0\right)$	e) NOTA			
22	If $\frac{x}{y} = \frac{3}{5}$, what is the	e value of the expression	on $\frac{x-5y}{y}$?					
	a) $-\frac{22}{5}$	b) $-\frac{2}{5}$	c) 0	d) $\frac{5}{3}$	e) NOTA			
23	23. What is the lowest common multiple of $72a^5b^6c^3$, $48a^6b^{10}c^7$, and $60a^3c^9d$?							
	a) $12a^3c^3$	b) $360a^6b^{10}c^9$	c) $720a^6b^{10}c^9$	d) $1440a^6b^{10}c^9d$	e) NOTA			
24	Jimmy has \$16.40 in pennies, nickels, dimes, and quarters. He has an equal number of each coin. How many total coins does he have?							
	a) 5	b) 12	c) 8	d) 16	e) NOTA			



c) II only

d) II and IV

e) NOTA

30. Which list of quadrants contains all the solutions to the system $y > 2, x \le -3$?

b) III only

a) II, III, & IV

Question #1

Find the value of the expression $a^b(b^a \cdot a^a \cdot 7 - 1)$, given a = 2 and b = 3.

Question #2

What is the power of x in the simplified form of: $\frac{\left(-3x^{5}y^{10}z^{7}\right)^{4} \cdot \left(25x^{8}y^{6}z^{3}\right)^{6}}{\left(9x^{2}y^{6}z^{8}\right)^{3} \cdot \left(-5x^{9}y^{3}z^{11}\right)^{5}}$

Question #3

What is the sum of the solutions of the three equations below?

$$5x - (12x - 8) + 3 = 2x + 29$$

$$\frac{2x + 7}{2} = \frac{-5x - 2}{4}$$

$$9x^2 - 16x + 7 = 0$$

Question #4

Let A = the value of a such that the line containing (a, 3) and (-2, 7) has slope $\frac{5}{3}$.

Let \mathbf{B} = the y-intercept of the line containing (-3, 3) and parallel to 2x - 3y = 10.

Let C = the x-intercept of the line containing (10, 1) and perpendicular to 2x - y = -4.

What is the value of $A \cdot B + C$?

Question #5

- A: A fraction has a value of 3/4. When the numerator is increased by 7, the resulting fraction equals the reciprocal of the original fraction.

 What is the denominator of the original fraction?
- **B**: The numerator of a certain fraction is a 2-digit number. The denominator is that number with the digits reversed. The value of the fraction is $\frac{4}{7}$. What is the numerator of the largest fraction that fits this description?

Find the value of $\frac{A}{B}$.

Question #6

Find the sum of the integral solutions of each of the following:

i)
$$[3x + 2] = 7$$

ii)
$$-5x+3 \ge 10$$
 and $4x-9 < 5x-4$

iii)
$$(3x+8)(x-5)(x+1)(x-10) = 0$$

Question #7 Simplify: $\sqrt{7,840,800}$

Question #8 Solve each of the following equations, and find the value of $r \cdot w - n + k$.

$$\frac{n+5}{12} - \frac{n+3}{8} = 1$$

$$\frac{3}{4}(2r+5) - \frac{5}{8}(3r-1) = 1$$

$$\frac{3w+5}{3} = 3w+2-\frac{3w-4}{6}$$

$$.03k + .05(1,000 - k) = 34$$

Question #9

Use long division to find the indicated quotients A and B. Find the sum A + B.

$$A = \frac{m^3 - 3m - 2}{m^2 + 2m + 1}$$

$$\boldsymbol{B} = \frac{8m^3 - 27}{2m - 3}$$

Question #10

Andy counted up some m&m's. He noticed that whether he sorts them in groups of 4's, 5's, or 7's, there are always 3 m&m's left over. What is the least number of m&m's that are possible for Andy to have?

Question #11

Find the sum of the abscissa and ordinates of the intersection points of each of the following pairs of lines:

$$4x - 7y = 8$$

$$5x - 4y = 2$$

The horizontal line containing (4, -5).

$$5x + 9y = 81$$
 $2x + 4y = 40$

$$2x + 4y = 40$$

The vertical line containing (-8, 2).

Question #12 If (x + y) = 4 and $(x^2 - y^2) = 12$, find the value of xy.

Question #13

Find the y-intercept of the line which contains the point (-6, 8) and which is also parallel to the line with equation 5x + 2y = 7.

Question #14

Using x = the smallest even prime number, and y = the smallest odd prime number,

find the value of the expression
$$xy^y[(xy)^x+1]+x^{xy}-xy^y$$

- 1. C Using order of operations: $2 + \frac{16}{3} 5 + 9 \Rightarrow 6 + \frac{16}{3} = 11\frac{1}{3}$
- 2. C
- 3. C $9x+3-x+1=6x+60 \Rightarrow 8x+4=6x+60 \Rightarrow 2x=56 \Rightarrow x=28$ Sum of digits is 10.
- 4. **B** $16y 16m = 8m 4y \Rightarrow 20y = 24m \Rightarrow y = \frac{6}{5}$
- 5. **B** $x+2=\frac{1}{3}x-4\Rightarrow \frac{2}{3}x=-6\Rightarrow x=-9$. So the integers are -9 and -7; their product is 63.
- 6. **B** $-6 < 5x 4 < 10 \Rightarrow -2 < 5x < 14 \Rightarrow -\frac{2}{5} < x < \frac{14}{5}$. The integral solutions are **0,1,2**; the sum is **3.**
- 7. **E** $-2x(-27x^3y^3) + 9x^2 \cdot x^2 \cdot y^2 \cdot -6y = 54x^4y^3 54x^4y^3 = 0$
- 8. A factors are (6x+7)(x-9) so the sum is 6+7+1-9=5
- 9. **B** Factor by grouping: $x(a-6y)-5(a-6y) \Rightarrow (x-5)(a-6y)$
- 10. B Factor as the difference of squares: $(x^2-9)(x^2+9) \rightarrow (x+3)(x-3)(x^2+9)$
- 11. **D** Conjugates: $(3x+5)(3x-5) \rightarrow 9x^2 25$; $(3x-5)^2 = 9x^2 30x + 25$. Subtracting gives us -30x + 50, with x = 5, we get -100
- 12. C Let u = units digit, and t = tens digit, then: u = 2 + t and 10u + t = 2(10t + u) 39. By solving this system, we get t = 5 and u = 7. The original number was 57. The product of the digits is 35.
- 13. **D** Let 4x = # of cats, 7x = # of dogs, x = # of turtles. Then 4x + 7x + x = 84; $\rightarrow x = 7$ and dogs = 49.
- 14. E Cross multiply $\Rightarrow 8x 12 = 15x 5 \Rightarrow x = -1$. Sub for x: $-2(-1)^5 7(-1)^4 + 3(-1)^3 + (-1) 5 = -14$
- 15. A $\left[-\frac{1}{2} + \frac{3}{5} + \frac{2}{3} \left(\frac{3}{10} \right) \right] \div \frac{1}{3} \frac{1}{9} \rightarrow \left[\frac{1}{10} + \frac{1}{5} \right] \div \frac{1}{3} \frac{1}{9} \rightarrow \left[\frac{3}{10} \right] \div \frac{1}{3} \frac{1}{9} = \frac{9}{10} \frac{1}{9} = \frac{71}{90}$. Difference is 19.
- 16. **B** Possibilities are: 4, 7, 8, 11, 12, 14, 15, 16, 18, 19, 20, 21. We have 4 consecutive integers, so all other whole numbers are possible by simply adding on 4 to prior values. Last impossible score is 17.
- 17. **D** One digit pages: 1-9=9 digits. Two digit pages: 10-99=90 pgs x 2=180 digits. Three digit pages: 100-759=660 pages x 3=1980 digits. Total digits = **2,169**.
- 18. **D** $(2^5)^x = 2^4 \rightarrow 2^{5x} = 2^4 \rightarrow 5x = 4 \rightarrow x = \frac{4}{5}$
- 19. **B** $\frac{-1-4}{x+2} = -\frac{3}{2}$. Cross multiplying, $-10 = -3x 6 \Rightarrow x = \frac{4}{3}$
- 20. A Eliminate x by subtracting the equations, so $-7y = 6 \Rightarrow y = -\frac{6}{7}$
- 21. C Given equation has slope of 15. $\pm slope = -\frac{1}{15}$. In point slope form, line L is: $y+5=-\frac{1}{15}(x-6)$. The x- intercept is found by replacing y with 0, giving us x=-69
- 22. A $\frac{x-5y}{y} = \frac{x}{y} \frac{5y}{y} \to \frac{3}{5} 5 = -\frac{22}{5}$
- 23. E $72 = 2^3 \cdot 3^2$; $48 = 2^4 \cdot 3$; $60 = 2^2 \cdot 3 \cdot 5$. LCM = $2^4 \cdot 3^2 \cdot 5 = 720$. Including variables: $720a^6b^{10}c^9d$
- 24. E A set of one of each coin = 41ϕ . $$16.40 \div 0.41 = 40$ sets of coins. Multiply by 4 coins = 160 total.
- 25. A Factor difference of two squares: $\frac{1,000 \cdot 1,000}{(254 246)(254 + 246)} \rightarrow \frac{1,000 \cdot 1,000}{(8)(500)} \rightarrow \frac{125 \cdot 2}{1 \cdot 1} = 250$
- 26. **B** $0 = 2x^2 5x 3 \rightarrow 0 = (2x + 1)(x 3)$. x intercepts are $-\frac{1}{2}$ and 3. The integers between are 0, 1, 2. 3

27. **D**
$$\frac{87 \cdot 6 + 3x}{9} = 92 \rightarrow x = 102$$

28. A Set up a system of equations and solve by substitution:

$$10.8a + 7.8w + 3.9p = 6(21)$$
 $a + w + p = 21$ $p = 2w$.

First substitute and get a + 3w = 21, then use a = 21 - 3w and substitute into long equation:

$$10.8(21-3w)+7.8w+3.9(2w)=126$$
. This solves and gives us $w=6$, so $a=3$.

29. D

$$f(-3) = 5 - 2 \cdot 9 = -13$$

 $h(-13) = |-26 - 3| = 29$
 $g(29) = 24/2 = 12$

30. C The solution lies above the horizontal line y = 2 and to the left of the vertical line x = -3. This intersection would be only in quadrant II.

1.
$$2^3(3^2 \cdot 2^2 \cdot 7 - 1) = 8(36 \cdot 7 - 1) = 8 \cdot 252 - 8 = 2008$$

2. Simplify only the factors of x:
$$\frac{x^{20} \cdot x^{48}}{x^6 \cdot x^{45}} = x^{14} \cdot x^3 = x^{17} \Longrightarrow 17$$

3. First equation: Second equation: (cross multiply first)
$$5x - (12x - 8) + 3 = 2x + 29$$

$$-7x + 8 + 3 = 2x + 29$$

$$-18 = 9x$$

$$x = -2$$
Second equation: (factor first)
$$8x + 28 = -10x - 4$$

$$18x = -32$$

$$9x - 7 = 0$$

$$x = -16$$

$$x = -\frac{16}{9}$$

$$x = -\frac{16}{9}$$

$$x = -\frac{7}{9}$$

$$x = 1$$

The sum of all these solutions is -2.

4. A:
$$\frac{7-3}{-2-a} = \frac{5}{3} \rightarrow 12 = -10 - 5a \Rightarrow a = -\frac{22}{5}$$
 B: $m = \frac{2}{3}$; $3 = \frac{2}{3}(-3) + b$, so $b = 5$

C: m = 2, so $\pm m = -\frac{1}{2}$. Using point-slope form and y = 0; $-1 = -\frac{1}{2}(x - 10)$, so x = 12. A+B+C = -10

5. A: Set up with
$$\frac{n}{d} = \frac{3}{4}$$
 and $\frac{n+7}{d} = \frac{4}{3}$. Cross multiply; solve the resulting system: $\frac{3d-4n=0}{4d-3n=21} \Rightarrow d=12$

B:
$$\frac{10t+u}{10u+t} = \frac{4}{7}$$
 Cross multiply and simply to: $u = 2t$. Solutions are 12, 24, 36, and 48; largest is 48. $\frac{A}{B} = \frac{1}{4}$

- 6. i) Solve $3x + 2 = \pm 7$ The integral solution is $\{-3\}$. ii) $x \le -\frac{7}{5}$ and x > -5, so integers are -4, -3, and -2. iii) Solutions are $-\frac{8}{3}$, 5, -1, and 10. The sum requested is -3 + -4 + -3 + -2 + -1 + 5 + 10 = 2.
- 7. Factor, using perfect squares wherever possible: $7,840,800 = 100 \cdot 78,408 = 100 \cdot 8 \cdot 9801 = 100 \cdot 8 \cdot 9 \cdot 1089 = 100 \cdot 8 \cdot 9 \cdot 9 \cdot 121$. Taking the square root of these factors, we get $10 \cdot 2 \cdot 9 \cdot 11\sqrt{2} \Rightarrow 1980\sqrt{2}$

8. *n*: Multiply equation by 24, getting
$$2n+10-3n-9=24$$
, so $n=-23$
r: multiply equation by 8, getting $12r+30-15r+5=8$, so $r=9$
w: multiply by 6, getting $6w+10=18w+12-3w+4$, so $w=-\frac{2}{3}$
k: multiply by 100, getting $3k+5(1,000-k)=3,400$. This solves to $k=800$. So: $9\cdot-\frac{2}{3}-\frac{2}{3}+800=817$.

9. By long division:
$$A = m - 2$$
 and $B = 4m^2 + 6m + 9$, so $A + B = 4m^2 + 7m + 7$

10. The lowest common multiple of 4, 5, and 7 is 140. Andy has 3 more than that, or 143 m&m's.

11.

$$\frac{4x - 7y = 8}{5x + 9y = 81} \Rightarrow \frac{-20x + 35y = -40}{20x + 36y = 324} \Rightarrow y = 4, x = 9 \rightarrow sum of these = 13$$

$$5x - 4y = 2$$

$$2x + 4y = 40$$
 $\Rightarrow x = 6, y = 7 \rightarrow sum \ of \ these = 13$

The horizontal and vertical lines intersect at (-8, -5); their sum = -13.

The sum of all these coordinates is 13.

12. Factoring and substituting, we get:

$$x^{2} - y^{2} = 12$$

$$(x+y)(x-y) = 12$$

$$4(x-y) = 12$$
Using the two equations
$$x-y=3$$

$$x+y=4$$
 we obtain
$$x = \frac{7}{2}, y = \frac{1}{2}$$
. The product $xy = \frac{7}{4}$

$$x-y=3$$

13. The line we want has the same slope as that of the given line, which is m = -5/2. Using point slope form, we can substitute in the slope, the point (-6, 8) and a value of 0 for x, since we want the y-intercept.

$$y-8 = -\frac{5}{2}(x+6) \rightarrow y-8 = -\frac{5}{2}(6) \Rightarrow y = -7$$

14. Substituting, with x = 2, and y = 3, we have

$$2 \cdot 3^{3} \left[(6)^{2} + 1 \right] + 2^{6} - 2 \cdot 3^{3}$$

$$= 54(37) + 64 - 54$$

$$= 1998 + 10$$

$$= 2008 \quad deja \ vu!!!$$