Chapter 8: Estimating with Confidence

Key Vocabulary:

- point estimator
- point estimate
- . confidence interval
- . margin of error
- . interval
- confidence level
- random
- normal

- independent
- four step process
- . level C confidence interval
- . degrees of freedom
- . standard error
- . one -sample z interval

- t distribution
- t-procedures

- one-sample t interval robust



8.1 **Confidence Intervals: The Basics (pp.615-643)**

- 1. A *point estimator* is a statistic that...
- 2. The value of the point estimator statistic is called a _____ and it is our

"best guess" at the value of the ______.

3. Summarize the facts about *sampling distributions* learned in chapter 7:

Shape

Center

Spread

- 4. In statistics, what is meant by a 95% *confidence interval*?
- 5. A confidence interval takes the form of : "estimate ± margin of error" where: estimate = margin of error =
- 6. Define a *level C confidence interval*.
- 7. What information does the margin of error provide?
- 8. Sketch and label a 95% confidence interval for the standard normal curve.
- 9. In a sampling distribution of \overline{x} , why is the interval of numbers between $\overline{x} \pm 2s$ called a 95% *confidence interval*?
- 10. Sketch and label a 90% confidence interval for the standard normal curve.
- 11. Interpret a Confidence level: "To say that we are 95% confident is shorthand for
- 12. Explain how to interpret a Confidence interval.
- 13. Does the confidence level tell us the chance that a particular confidence interval captures the population parameter? If not, what does it tell us?

14. What does the *critical value* depend on?

15. Write the *form* for calculating a confidence interval as shown on page 478.

16. Why do we want high confidence and a small margin of error?

17. Explain the two conditions when the margin of error gets smaller.

18. State the three conditions for constructing a confidence interval for p or μ .

- Random
- Normal
- Independent

19. What are the two important reminders for constructing and interpreting confidence intervals?

8.2 Estimating a Population Proportion (pp.484-494)

- 1. In statistics, what is meant by a *sample proportion:* \hat{p} ?
- 2. Give the mean and standard deviation for the sampling distribution of \hat{p} ?
- 3. How does the standard deviation differ to to standard error for the sampling distribution of \hat{p} ?
- 4. Describe the sampling distribution of a sample proportion \hat{p} as learned in section 7.2.
 - Shape
 - Center
 - Spread
- 5. Define *standard error*.
- 6. In general what is meant by the standard error of a statistic?
- 7. How do you calculate the standard error of \hat{p} ?
- 8. What is the formula for a *one-sample z interval for a population proportion*? Describe how to construct a level C confidence interval for a population proportion.

- 9. Describe the four step process on how to contruct and interpret a confidence interval.
 - State
 - Plan
 - Do
 - Conclude

10. What formula is used to determine the sample size necessary for a given margin of error?

11. What conditions must be met in order to use *z procedures* for inference about a proportion?

- 12. What does z^* represent?
- 13. What is the value of z^* for a 95% confidence interval? Include a sketch.
- 14. What is the value of z^* for a 90% confidence interval? Include a sketch.
- 15. What is the value of z^* for a 99% confidence interval? Include a sketch.

8.3 Estimating a Population Mean (pp.499-515)

- 1. What is the formula for a *one-sample z interval for a population mean*? Describe how to construct a level C confidence interval for a population mean.
- 2. What is the formula for the margin of error of the confidence interval for the population mean μ ?
- 3. How can you arrange to have both high confidence and a small margin of error?
- 4. Describe the three steps for choosing a sample size for a desired margin of error when estimating μ .
- 5. What happens to the *margin of error* as z^* gets smaller? Does this result in a higher or lower confidence level?
- 6. What happens to the *margin of error*, as σ gets smaller?
- 7. What happens to the *margin of error*, as *n* gets larger? By how many times must the sample size *n* increase in order to cut the *margin of error* in half?
- 8. The formula used to determine the sample size *n* that will yield a confidence interval for a population mean with a specified margin of error *m* is $z * \frac{\sigma}{\sqrt{n}} \le ME$. Solve for *n*.

9. It is the size of the ______ that determines the margin of error. The size of the ______ does not influence the sample size we need.

10. Complete the Check Your Undertanding on page 501.

- 11. How do you calculate the *degrees of freedom* for a *t distribution*?
- 12. What happens to the *t* distribution as the degrees of freedom increase?
- 13. How would you construct a t distribution?
- 14. Describe the differences between a standard normal distribution and a t distribution.
- 15. Describe the similarities between a standard normal distribution and a t distribution.
- 16. What is the formula for the *standard deviation* of the sampling distribution of the sample mean \overline{x} ?
- 17. What is the *standard error* of the sample mean \overline{x} ?
- 19. Describe how to construct the *one-sample t interval for a population mean*?

20. Summarize the *three conditions for inference about a population mean:*

- Random
- Normal
- Independent

21. Inferences for *proportions* use _____ and inferences for *means* use _____.

22. What does it mean if an inference procedure is **robust**?

23. If the size of the SRS is less than 15, when can we use t procedures on the data?

24. If the size of the SRS is at least 15, when can we use t procedures on the data?

25. If the size of the SRS is at least 30, when can we use t procedures on the data?

26. Summarize the details of the four step procedure for estimating *p*:

- State
- Plan
- Do
- Conclude